

$x^4 - 8224x^3 + 25360856x^2 - 34775906944x + 17860393921680 = 0$



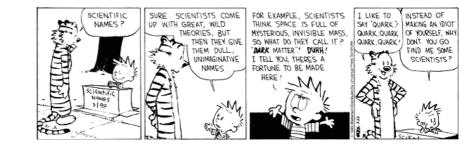
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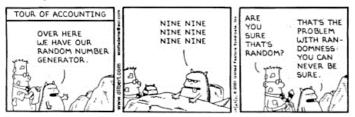


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DILBERT By Scott Adams



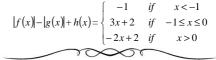
	1	W		RM132
			(1878) Agner Krarup Erlang	DM100
			(1894) Satyendranath Bose (1912) Boris Gnedenko	RM168
	2	т	(1822) Rudolf Julius Emmanuel Clausius	
			(1905) Lev Genrichovich Shnirelman	
			(1938) Anatoly Samoilenko	
	3	F	(1917) Yuri Alexeievich Mitropolsky	
	4	S	(1643) Isaac Newton	RM071
	5	\mathbf{S}	(1723) Nicole-Reine Etable de Labrière Lepaute (1838) Marie Ennemond Camille Jordan	
			(1836) Marie Ennemond Camille Jordan (1871) Federigo Enriques	RM084
			(1871) Gino Fano	1111001
2	6	М	(1807) Jozeph Mitza Petzval	
			(1841) Rudolf Sturm	
	7	Т	(1871) Felix Edouard Justin Emile Borel	
	0	***	(1907) Raymond Edward Alan Christopher Paley	DM150
	8	W	(1888) Richard Courant (1924) Paul Moritz Cohn	RM156
			(1924) Stephen William Hawking	
	9	Т	(1864) Vladimir Adreievich Steklov	
			(1915) Mollie Orshansky	
	10	F	(1875) Issai Schur	
		a	(1905) Ruth Moufang	Distan
	11	\mathbf{S}	(1545) Guidobaldo del Monte	RM120
			(1707) Vincenzo Riccati (1734) Achille Pierre Dionis du Sejour	
	12	\mathbf{S}	(1906) Kurt August Hirsch	
			(1915) Herbert Ellis Robbins	RM156
3	13	М	(1864) Wilhelm Karl Werner Otto Fritz Franz Wien	
			(1876) Luther Pfahler Eisenhart	
			(1876) Erhard Schmidt	
	14	т	(1902) Karl Menger (1902) Alfred Tarski	RM096
	14	w		101030
	10		(1717) Mattew Stewart	
			(1850) Sofia Vasilievna Kovalevskaja	RM144
	16	Т	(1801) Thomas Klausen	
	17	F	(1647) Catherina Elisabetha Koopman Hevelius	
			(1847) Nikolay Egorovich Zukowsky (1858) Gabriel Koenigs	
	18	\mathbf{S}	(1856) Luigi Bianchi	
	10	~	(1880) Paul Ehrenfest	
	19	\mathbf{S}	(1813) Rudolf Friedrich Alfred Clebsch	
			(1879) Guido Fubini	
	00	ъл	(1908) Aleksandr Gennadievich Kurosh	
4	20	М	(1775) André Marie Ampère (1895) Gabor Szegő	
			(1994) Renato Caccioppoli	RM072
	21	Т	(1846) Pieter Hendrik Schoute	101012
			(1915) Yuri Vladimirovich Linnik	
	22	W		
			(1886) John William Navin Sullivan	DMOGO
	23	т	(1908) Lev Davidovich Landau (1840) Ernst Abbe	RM063
	4J	Ŧ	(1862) David Hilbert	RM060
	24	\mathbf{F}	(1891) Abram Samoilovitch Besicovitch	1.1000
			(1914) Vladimir Petrovich Potapov	
	25	\mathbf{S}	(1627) Robert Boyle	
			(1736) Joseph-Louis Lagrange	RM048
	26	\mathbf{S}	(1843) Karl Hermann Amandus Schwarz (1799) Benoît Paul Émile Clapeyron	
	20	5	(1862) Eliakim Hastings Moore	
5	27	М	(1832) Charles Lutwidge Dodgson	RM108
	28	Т	(1701) Charles Marie de La Condamine	
			(1888) Louis Joel Mordell	
		***	(1892) Carlo Emilio Bonferroni	
	29	W		
	30	т	(1888) Sidney Chapman (1619) Michelangelo Ricci	
	31	F	(1715) Giovanni Francesco Fagnano dei Toschi	
		-	(1841) Samuel Loyd	
			(1896) Sofia Alexandrovna Janowskaja	
			(1945) Persi Warren Diaconis	
			(1900) John Charles Burkill (1522) Lodovico Ferrari	
L			(1022) LOUOVICO FEITAII	



January

Putnam 1999, A1

Find polynomials f(x), g(x) and h(x), if they exist, such that for all x:



The Amazing U

"Has anyone had problems with the computer accounts?"

"Yes, I don't have one."

"Okay, you can send mail to one of the tutors..."

- E. D'Azevedo Computer Science 372

Weird, but true

The First Law of Applied Mathematics: All infinite series converge, and moreover converge to the first term.

Wir müssen wissen. Wir werden wissen. (We must know. We will know).

[Speech in Königsberg in 1930, now on his tomb in Göttingen]

David Hilbert

Galileo was no idiot. Only an idiot could believe that science requires martyrdom – that may be necessary in religion, but in time a scientific result will establish itself.

David Hilbert

The reader will find no figures in this work. The methods which I set forth do not require either constructions or geometrical or mechanical reasonings: but only algebraic operations, subject to a regular and uniform rule of procedure.

Joseph-Louis Lagrange

We lay down a fundamental principle of generalization by abstraction: "The existence of analogies between central features of various theories implies the existence of a general theory which underlies the particular theories and unifies them with respect to those central features...."

Eliakim Hastings Moore

Mathematical study and research are very suggestive of mountaineering. Whymper made several efforts before he climbed the Matterhorn in the 1860's and even then it cost the life of four of his party. Now, however, any tourist can be hauled up for a small cost, and perhaps does not appreciate the difficulty of the original ascent. So in mathematics, it may be found hard to realise the great initial difficulty of making a little step which now seems so natural and obvious, and it may not be surprising if such a step has been found and lost again. Louis Joel Mordell

	-	a		
	1	S	(1900) John Charles Burkill	
	2	\mathbf{S}	(1522) Lodovico Ferrari	
			(1893) Cornelius Lanczos (1897) Gertrude Blanch	
6	3	м	(1893) Gaston Maurice Julia	RM073
0		M		KM073
	4	T	(1905) Eric Cristopher Zeeman	
	5	W	(1757) Jean Marie Constant Duhamel	DMOOL
	6	Т	(1465) Scipione del Ferro	RM064
			(1612) Antoine Arnauld	DMOOD
	-	Б	(1695) Nicolaus (II) Bernoulli	RM093
	7	F	(1877) Godfried Harold Hardy	RM049
	0	G	(1883) Eric Temple Bell	DM009
	8	\mathbf{S}	(1700) Daniel Bernoulli (1875) Francis Ysidro Edgeworth	RM093
				DM199
	0	G	(1928) Ennio de Giorgi	RM133
	9	\mathbf{S}	(1775) Farkas Wolfgang Bolyai	DM007
7	10	М	(1907) Harold Scott Macdonald Coxeter (1747) Aida Yasuaki	RM097 RM121
1	10	IVI	(1747) Alda Tasuaki (1932) Vivienne Malone-Mayes	N W1121
	11	т	(1552) Vivienne Majone-Mayes (1657) Bernard Le Bovier de Fontenelle	
	11	1	(1800) William Henry Fox Talbot	
			(1839) Josiah Willard Gibbs	
			(1915) Richard Wesley Hamming	
	12	w	(1914) Hanna Caemmerer Neumann	
	14	••	(1921) Kathleen Rita Mcnulty Mauchly Antonelli	
	13	т	(1805) Johann Peter Gustav Lejeune Dirichlet	RM145
	14	F	(1468) Johann Werner	1001110
		•	(1849) Hermann Hankel	
			(1877) Edmund Georg Hermann Landau	RM063
			(1896) Edward Artur Milne	
	15	\mathbf{S}	(1564) Galileo Galilei	RM085
			(1850) Sophie Willock Bryant	
			(1861) Alfred North Whitehead	
			(1946) Douglas Hofstadter	
	16	\mathbf{S}	(1822) Francis Galton	
			(1853) Gregorio Ricci-Curbastro	
			(1903) Beniamino Segre	
8	17	М	(1890) Sir Ronald Aylmer Fisher	
			(1891) Adolf Abraham Halevi Fraenkel	
		_	(1905) Rózsa Péter	
	18	Т	(1404) Leon Battista Alberti	RM157
	10	***	(1919) Clifford Truesdell	
	19	W	(1473) Nicolaus Copernicus	DMOOT
	20	Т	(1844) Ludwig Boltzmann	RM061
	21	F	(1591) Girard Desargues (1015) Frances Michaelanich Lifshitz	
		c	(1915) Evgeny Michailovich Lifshitz	
1	22	\mathbf{S}	(1857) Heinrich Rudolf Hertz (1992) Frank Blausster Bausser	
		a	(1903) Frank Plumpton Ramsey	
	23	\mathbf{S}	(1583) Jean-Baptiste Morin	
1			(1922) Anneli Cahn Lax (1951) Shirachumi Mani	
			(1951) Shigefumi Mori (1561) Henry Briggs	RM169
9	91	М	(1961) Henry Briggs (1871) Felix Bernstein	1011109
9	24 25	Т		
		W	(1827) Henry Watson	
	26 27		(1786) Dominique Francois Jean Arago (1881) Luitzen Egbertus Jan Brouwer	
	27 29	T F	(1735) Alexandre Theophile Vandermonde	
	28 29	r	(1735) Alexandre Theophile Vandermonde (1860) Herman Hollerith	RM109
L	49			101109





Putnam 1999, A2

Let p(x) be a polynomial that is nonnegative for all real x. Prove that for some k, there are polynomials $f_1(x), \ldots, f_k(x)$ such that:

$$p(x) = \sum_{j=1}^{k} (f_j(x))^2$$

The Amazing U

"If that makes any sense to you, you have a big problem."

- C. Durance Computer Science 234

Weird, but true

There are two groups of people in the world: those who believe that the world can be divided into two groups of people, and those who don't.

It is the perennial youthfulness of mathematics itself which marks it off with a disconcerting immortality from the other sciences.

Eric Temple Bell

"Obvious" is the most dangerous word in mathematics. Eric Temple Bell

Finally we shall place the Sun himself at the center of the Universe. All this is suggested by the systematic procession of events and the harmony of the whole Universe, if only we face the facts, as they say, 'with both eyes open'.

Nicolaus Copernicus

Mathematicians are like lovers. Grant a mathematician the least principle, and he will draw from it a consequence which you must also grant him, and from this consequence another.

Bernard Le Bovier De Fontenelle

Does anyone believe that the difference between the Lebesgue and Riemann integrals can have physical significance, and that whether say, an airplane would or would not fly could depend on this difference? If such were claimed, I should not care to fly in that plane.

Richard Wesley Hamming

	1	\mathbf{S}	(1611) John Pell	
	2	\mathbf{S}	(1879) Robert Daniel Carmichael (1836) Julius Weingarten	
10	3	M	(1838) George William Hill	
_			(1845) Georg Cantor	RM062
		_	(1916) Paul Richard Halmos	
	4 5	T W	(1822) Jules Antoine Lissajous (1512) Gerardus Mercator	
	Э	vv	(1512) Gerardus Mercator (1759) Benjamin Gompertz	
			(1817) Angelo Genocchi	
			(1885) Pauline Sperry	
			(1915) Laurent Schwartz	
	6	т	(1931) Vera Pless (1866) Ettore Bortolotti	
	7	F	(1792) William Herschel	RM146
			(1824) Delfino Codazzi	
			(1922) Olga Alexandrovna Ladyzhenskaya	
	8 9	s s	(1851) George Chrystal (1818) Ferdinand Joachimsthal	
	9	Э	(1818) Ferdinand Joachimsthal (1900) Howard Hathaway Aiken	
11	10	Μ	(1864) William Fogg Osgood	
			(1872) Mary Ann Elizabeth Stephansen	
	11	Т	(1811) Urbain Jean Joseph Le Verrier	
			(1853) Salvatore Pincherle (1870) Louis Bachelier	RM158
	12	w	(1685) George Berkeley	1001150
			(1824) Gustav Robert Kirchhoff	
		_	(1859) Ernesto Cesaro	
	13	Т	(1861) Jules Joseph Drach (1957) Rudy D'Alembert	
	14	F	(1957) Kudy D'Alembert (1864) Jozef Kurschak	
		-	(1879) Albert Einstein	RM074
			(1904) Lyudmila Vsevolodovna Keldysh	
	15	\mathbf{S}	(1860) Walter Frank Raphael Weldon	
	16	\mathbf{S}	(1868) Grace Chisolm Young (1750) Caroline Herschel	RM146
	10	D	(1789) Georg Simon Ohm	1011140
			(1846) Magnus Gosta Mittag-Leffler	
12	17	М	(1876) Ernest Benjamin Esclangon	
	18	т	(1897) Charles Fox (1640) Philippe de La Hire	
	10	•	(1690) Christian Goldbach	RM122
			(1796) Jacob Steiner	
	10	***	(1870) Agnes Sime Baxter	
	19	W	(1862) Adolf Kneser (1910) Jacob Wolfowitz	
	20	Т	(1840) Franz Mertens	
			(1884) Philip Franck	
		-	(1938) Sergi Petrovich Novikov	
	21	F	(1768) Jean Baptiste Joseph Fourier (1884) George David Birkhoff	
	22	\mathbf{S}	(1891) Lorna Mary Swain	
			(1917) Irving Kaplansky	
		C	(1944) Margaret Hilary Ashworth Millington	
	23	\mathbf{S}	(1754) Georg Freiherr von Vega (1882) Emmy Amalie Noether	RM050
			(1897) John Lighton Synge	10101000
13	24	М	(1809) Joseph Liouville	
			(1948) Sun-Yung (Alice) Chang	DM1 (A
	25	Т	(1966) Gigliola Staffilani (1538) Christopher Clausius	RM142
	25 26	W	(1956) Christopher Clausius (1848) Konstantin Andreev	
	-		(1913) Paul Erdős	RM110
	27	Т	(1857) Karl Pearson	
	28	F	(1749) Pierre-Simon de Laplace (1928) Alexander Grothendieck	DMOOD
	29	\mathbf{S}	(1928) Alexander Grotnendleck (1825) Francesco Faà Di Bruno	RM086 RM170
		~	(1873) Tullio Levi-Civita	RM098
			(1896) Wilhelm Ackerman	
	30	\mathbf{S}	(1892) Stefan Banach (1921) Alfréd Bényri	RM134
14	31	м	(1921) Alfréd Rényi (1596) René Descartes	
14	91	111	(1000) 10110 Descur 100	



March

Putnam 1999, A3

Consider the power series expansion:

$$\frac{1}{1-2x-x^2} = \sum_{n=0}^{\infty} a_n x^n$$

Prove that, for each integer $n \ge 0$, there is an integer m such that $a^{2_n} + a^{2_{n+1}} = a_m$.

The Amazing U

"Let's make ethanol green this afternoon."

- R. Friesen Chemistry 124

Weird, but true

Theorem: All the numbers are boring Proof (by contradiction): Suppose x is the first non-boring number. Who cares?

He who can digest a second or third fluxion, a second or third difference, need not, we think, be squeamish about any point of divinity.

George Berkeley

If I found any new truths in the sciences, I can say that they follow from, or depend on, five or six principal problems which I succeeded in solving and which I regard as so many battles where the fortunes of war were on my side.

René Descartes

(During a lecture) *This has been done elegantly by Minkowski; but chalk is cheaper than grey matter, and we will do it as it comes.*[Attributed by Pólya.]

Albert Einstein

I remember one occasion when I tried to add a little seasoning to a review, but I wasn't allowed to. The paper was by Dorothy Maharam, and it was a perfectly sound contribution to abstract measure theory. The domains of the underlying measures were not sets but elements of more general Boolean algebras, and their range consisted not of positive numbers but of certain abstract equivalence classes. My proposed first sentence was: "The author discusses valueless measures in pointless spaces."

Paul Richard Halmos

Read Euler: he is our master in everything.

Pierre-Simon De Laplace

If one proves the equality of two numbers a and b by showing first that 'a is less than or equal to b' and then 'a is greater than or equal to b', it is unfair, one should instead show that they are really equal by disclosing the inner ground for their equality.

Emmy Amalie Noether

	1	Т	(1640) Georg Mohr	
			(1776) Marie-Sophie Germain	
	•		(1895) Alexander Craig Aitken	
	2	W	(1878) Edward Kasner	
	3	т	(1934) Paul Joseph Cohen (1835) John Howard Van Amringe	
	3	T	(1892) Hans Rademacher	
			(1900) Albert Edward Ingham	
			(1909) Stanislaw Marcin Ulam	RM171
			(1971) Alice Riddle	
	4	\mathbf{F}	(1809) Benjamin Peirce	RM123
			(1842) Francois Edouard Anatole Lucas	
	-	a	(1949) Shing-Tung Yau	
	5	\mathbf{S}	(1588) Thomas Hobbes (1607) Honoré Fabri	
			(1607) Hohore Fabri (1622) Vincenzo Viviani	
			(1869) Sergi Alexeievich Chaplygin	
	6	\mathbf{S}	(1801) William Hallowes Miller	
15	7	М	(1768) François-Joseph Français	
	8	Т	(1903) Marshall Harvey Stone	
	9	W	(1791) George Peacock	
			(1816) Charles Eugene Delaunay	
			(1894) Cypra Cecilia Krieger Dunaij	
	10	т	(1919) John Presper Heckert (1857) Henry Ernest Dudeney	
	11	T F	(1953) Andrew John Wiles	
	12	S	(1794) Germinal Pierre Dandelin	
		N	(1852) Carl Louis Ferdinand von Lindemann	
			(1903) Jan Tinbergen	
	13	\mathbf{S}	(1728) Paolo Frisi	
			(1813) Duncan Farquharson Gregory	
			(1869) Ada Isabel Maddison	
16	14	м	(1879) Francesco Severi (1629) Christiaan Huygens	DM195
10	14 15	M T	(1452) Leonardo da Vinci	RM135
	10	T	(1528) Pietro Antonio Cataldi	
			(1707) Leonhard Euler	RM051
			(1809) Herman Gunther Grassmann	
	16	W	(1682) John Hadley	
		-	(1823) Ferdinand Gotthold Max Eisenstein	
	17	Т	(1798) Etienne Bobillier	
			(1853) Arthur Moritz Schonflies (1863) Augustus Edward Hough Love	
	18	F	(1791) Ottaviano Fabrizio Mossotti	RM150
	10	-	(1907) Lars Valerian Ahlfors	1001100
			(1918) Hsien Chung Wang	
			(1949) Charles Louis Fefferman	
	19	\mathbf{S}	(1880) Evgeny Evgenievich Slutsky	
			(1883) Richard von Mises	
			(1901) Kiyoshi Oka (1905) Charles Ebreamann	
	20	\mathbf{S}	(1905) Charles Ehresmann (1839) Francesco Siacci	
17	20	M	(1652) Michel Rolle	
	-	-	(1774) Jean Baptiste Biot	
			(1875) Teiji Takagi	
	22	Т	(1811) Otto Ludwig Hesse	
			(1887) Harald August Bohr	RM063
			(1935) Bhama Srinivasan (1939) Sir Michael Francis Atiyah	
	23	w	(1858) Max Karl Ernst Ludwig Planck	
	20	••	(1910) Sheila Scott Macintyre	
	24	Т	(1863) Giovanni Vailati	
			(1899) Oscar Zariski	RM099
	25	\mathbf{F}	(1849) Felix Christian Klein	
			(1900) Wolfgang Pauli	
		~	(1903) Andrei Nicolayevich Kolmogorov	RM159
	26 27	S	(1889) Ludwig Josef Johan Wittgenstein	
	27	\mathbf{S}	(1755) Marc-Antoine Parseval des Chenes (1932) Gian-Carlo Rota	
18	28	М	(1962) Gran-Carlo Inita (1906) Kurt Godel	RM087
	20 29	Т	(1854) Jules Henri Poincarè	RM0075
	30	W		RM147
			(1916) Claude Elwood Shannon	RM111



April

Putnam 1999, A4 Sum the series:

 m^2n $n3^{m} + m3^{n}$

The Amazing U

"You can write a small letter to Grandma in the filename."

- Forbes Burkowski Computer Science 454

Weird, but true

It is proven that celebration of birthdays is healthy. Statistics show that those people that celebrate the most birthdays become the oldest.

Mathematicians have tried in vain to this day to discover some order in the sequence of prime numbers, and we have reason to believe that it is a mystery into which the human mind will never penetrate.

Leonhard Euler

[numbers as the square root of minus one] are neither nothing nor something less than nothing, which makes them necessarily imaginary, or impossible.

Leonhard Euler

We must admit with humility that, while number is purely a product of our minds, space has a reality outside our minds, so that we cannot completely prescribe its properties a priori.

Johann Carl Friedrich Gauss

I have had my results for a long time: but I do not yet know how I am to arrive at them.

Johann Carl Friedrich Gauss

There is no certainty in sciences where one of the mathematical sciences cannot be applied, or which are not in relation with these mathematics.

Leonardo Da Vinci

Benjamin Peirce

The riddle does not exist. If a question can be put at all, then it can also be answered.

Ludwig Josef Johan Wittgenstein

	1	Т	(1825) Johann Jacob Balmer	RM122
	_	_	(1908) Morris Kline	
	2	\mathbf{F}	(1860) D'Arcy Wentworth Thompson	RM138
			(1905) Kazimierz Zarankiewitz	
	3	\mathbf{S}	(1842) Otto Stolz	
			(1860) Vito Volterra	RM136
			(1892) George Paget Thomson	RM161
	4	\mathbf{S}	(1845) William Kingdon Clifford	
19	5	Μ	(1833) Lazarus Emmanuel Fuchs	
			(1883) Anna Johnson Pell Wheeler	
			(1897) Francesco Giacomo Tricomi	
			(1923) Cathleen Synge Morawetz	
	6	Т	(1872) Willem de Sitter	
	_		(1906) André Weil	RM088
	7	W	(1854) Giuseppe Veronese	
			(1881) Ebenezer Cunningham	
			(1896) Pavel Sergieievich Alexandrov	
	0	т	(1926) Alexis Claude Clairaut	
	8	Т	(1859) Johan Ludwig William Valdemar Jensen (1905) Winifred Lydia Caunden Sargent	
1	9	F	(1746) Gaspard Monge	
	3	г	(1876) Gilbert Ames Bliss	
			(1965) Karen Ellen Smith	
	10	\mathbf{S}	(1788) Augustin Jean Fresnel	
			(1847) William Karl Joseph Killing	
			(1904) Edward James Mcshane	
			(1958) Piotr Rezierovich Silverbrahms	
	11	\mathbf{S}	(1902) Edna Ernestine Kramer Lassar	
			(1918) Richard Phillips Feynman	RM076
20	12	м	(1820) Florence Nightingale	RM104
			(1845) Pierre René Jean Baptiste Henry Brocard	
	10	m	(1902) Frank Yates	
	13	Т	(1750) Lorenzo Mascheroni (1800) Palaggia Vakaylayna Palyharingya Kashina	
	14	w	(1899) Pelageia Yakovlevna Polubarinova Kochina (1832) Rudolf Otto Sigismund Lipschitz	
	14	**	(1863) John Charles Fields	RM100
	15	Т	(1939) Brian Hartley	1001100
	10	-	(1964) Sijue Wu	
	16	\mathbf{F}	(1718) Maria Gaetana Agnesi	RM112
			(1821) Pafnuti Lvovi Chebyshev	
			(1911) John (Jack) Todd	RM139
	17	\mathbf{S}	(1940) Alan Kay	
1	18	\mathbf{S}	(1850) Oliver Heaviside	RM160
			(1892) Bertrand Arthur William Russell	RM052
21	19	М	(1865) Flora Philip	
		m	(1919) Georgii Dimitirievich Suvorov	
	20	T	(1861) Henry Seely White	DM194
1	21	W		RM124
	22	Т	(1792) Gustave Gaspard de Coriolis (1865) Alfred Cardew Dixon	
	22 23	F	(1914) Lipa Bers	RM148
	$\frac{23}{24}$	г S	(1544) William Gilbert	1011140
1	$\frac{24}{25}$	S	(1838) Karl Mikailovich Peterson	
22	<u>25</u> 26	M	(1667) Abraham de Moivre	
	20	111	(1896) Yuri Dimitrievich Sokolov	
1			(1862) John Edward Campbell	
1	27	Т		
	$\frac{27}{28}$	T W		
	27 28	T W	(1676) Jacopo Francesco Riccati (1710) Johann (II) Bernoulli	RM093
			(1676) Jacopo Francesco Riccati	RM093
	28	W	(1676) Jacopo Francesco Riccati (1710) Johann (II) Bernoulli	RM093



May

Putnam 1999, A5

Prove that there is a constant C such that, if $p(x) \mathrm{is}$ a polynomial of degree 1999, then:

p(x)dx

The Amazing U

"What I've done, of course, is total garbage." - R. Willard Pure Math 430a.

Weird, but true

Statistics are like a bikini. What is revealed is interesting, what is concealed is crucial.

The trouble with maths is that you believe you know what you're aiming for: however - when you get there - not only you don't know where 'there' is, but you're not even anymore sure of where you started in the first place. Maurizio Codogno, Dotmaudot

I think that I can safely say that nobody understands quantum mechanics.

Richard Phillips Feynman

A proof tells us where to concentrate our doubts.

Morris Kline

Logic is the art of going wrong with confidence.

Morris Kline

Mathematics takes us into the region of absolute necessity, to which not only the actual word, but every possible word, must conform.

Bertrand Arthur William Russell

Every mathematician worthy of the name has experienced... the state of lucid exaltation in which one thought succeeds another as if miraculously... this feeling may last for hours at a time, even for days. Once you have experienced it, you are eager to repeat it but unable to do it at will, unless perhaps by dogged work....

André Weil

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				(1958) Abigail A Thompson	



June

Putnam 1999, A6

The sequence $(a_n)_{n\geq 1}$ is defined by $a_1=1$, $a_2=2$, $a_3=24$ and, for $n\geq 4$:

$$a_n = \frac{6a^{2_{n-1}}a_{n-3} - 8a_{n-1}a^{2_{n-2}}}{a_{n-2}a_{n-3}} \cdot$$

Show that, for all n, a_n is an integer multiple of n.

The Amazing U

"The algorithm to do that is extremely nasty. You might want to mug someone with it?"

- M. Devine Computer Science 340 50 \sim

Weird, but true

What's the question the Cauchy distribution hates the most? Got a moment?

[When asked about his age.] I was x years old in the year x^2 .

Augustus De Morgan

The purpose of models is not to fit the data but to sharpen the questions.

Samuel Karlin

I recall once saying that when I had given the same lecture several times I couldn't help feeling that they really ought to know it by now.

John Edensor Littlewood

Our notion of symmetry is derived from the human face. Hence, we demand symmetry horizontally and in breadth only, not vertically nor in depth.

Blaise Pascal

It can be of no practical use to know that π is irrational, but if we can know, it surely would be intolerable not to know.

Edward Charles Titchmarsh

This new integral of Lebesgue is proving itself a wonderful tool. I might compare it with a modern Krupp gun, so easily does it penetrate barriers which were impregnable.

Edward Burr Van Vleck

 T (1643) Gottfried Wilhelm von Leibniz (1788) Jean Victor Poncelet (1906) Jean Alexandre Eugène Dieudonné W (1820) William John Racquorn Rankine (1852) William Burnside (1925) Olga Arsen'evna Oleinik T (1807) Ernest Jean Philippe Fauque de Jonquiere (1897) Jesse Douglas 	RM054 RM162
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 2 W (1906) Jean Alexandre Eugène Dieudonné 2 W (1820) William John Racquorn Rankine (1852) William Burnside (1925) Olga Arsen'evna Oleinik 3 T (1807) Ernest Jean Philippe Fauque de Jonquiere (1897) Jesse Douglas 	RM162
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3 T (1807) Ernest Jean Philippe Fauque de Jonquiere (1897) Jesse Douglas	RM162
(1897) Jesse Douglas	RM162
4 F (1906) Daniel Edwin Rutherford	
(1917) Michail Samoilovich Livsic	
5 S (1936) James Mirrlees	
6 S (1849) Alfred Bray Kempe	
28 7 M (1816) Johann Rudolf Wolf	
(1906) William Feller	
(1922) Vladimir Aleksandrovich Marchenko	
8 T (1760) Christian Kramp	
(1904) Henri Paul Cartan	RM126
9 W (1845) George Howard Darwin	RM138
(1931) Valentina Mikhailovna Borok	1011100
10 T (1856) Nikola Tesla	RM174
	NN1174
(1862) Roger Cotes	
(1868) Oliver Dimon Kellogg	
11 F (1857) Sir Joseph Larmor	
(1888) Jacob David Tamarkin	RM101
(1890) Giacomo Albanese	
12 S (1875) Ernest Sigismund Fischer	
(1895) Richard Buckminster Fuller	RM066
(1935) Nicolas Bourbaki	RM126
13 S (1527) John Dee	
(1741) Karl Friedrich Hindenburg	
29 14 M (1671) Jacques D'Allonville	
(1793) George Green	RM078
15 T (1865) Wilhelm Wirtinger	101010
(1898) Mary Taylor Slow	
(1906) Adolph Andrej Pavlovich Yushkevich	
16 W (1678) Jakob Hermann (1009) Jakob Hermann	
(1903) Irmgard Flugge-Lotz	
17 T (1831) Victor Mayer Amedeè Mannheim	
(1837) Wilhelm Lexis	
(1944) Krystyna Maria Trybulec Kuperberg	
18 F (1013) Hermann von Reichenau	
(1635) Robert Hooke	RM114
(1853) Hendrik Antoon Lorentz	RM161
19 S (1768) Francois Joseph Servois	
20 S (1876) Otto Blumenthal	
(1947) Gerd Binnig	
30 21 M (1620) Jean Picard	
(1848) Emil Weyr	
(1849) Robert Simpson Woodward	
(1861) Herbert Ellsworth Slaught	
22 T (1784) Friedrich Wilhelm Bessel	
23 W (1775) Etienne Louis Malus	
(1854) Ivan Slezynsky	
24 T (1851) Friedrich Herman Schottky	
(1871) Paul Epstein	
(1923) Christine Mary Hamill	
25 F (1808) Johann Benedict Listing	
26 S (1903) Kurt Mahler	D1 (0
27 S (1667) Johann Bernoulli	RM093
(1801) George Biddel Airy	
(1848) Lorand Baron von Eötvös	
(1871) Ernst Friedrich Ferdinand Zermelo	RM090
31 28 M (1954) Gerd Faltings	
29 T (1898) Isidor Isaac Rabi	
30 W (1889) Vladimir Kosma Zworkyn	
31 T (1704) Gabriel Cramer	
(1712) Johann Samuel Koenig	
(1926) Hilary Putnam	
(1020) mary 1 uman	



July

Putnam 1999, B1

Right triangle *ABC* has right angle in *C* and *ABC*= θ ; the point *D* is chosen on *AB* so that |AC|=|AD|=1; the point *E* is chosen on *BC* so that $CDE=\theta$. The perpendicular to *BC* at *E* meets *AB* at *F*. Evaluate $\lim_{\theta \to 0} |EF|$.



The Amazing U

"Is it a really good acid, or just a half-acid?" - R. Friesen Chemistry 124

Weird, but true

Arguing with a statistician is a lot like wrestling with a pig. After a few hours you begin to realize the pig likes it.

Structures are the weapons of the mathematician. Nicolas Bourbaki

There is (gentle reader) nothing (the works of God only set apart) which so much beautifies and adorns the soul and mind of man as does knowledge of the good arts and sciences. ... Many ... arts there are which beautify the mind of man; but of all none do more garnish and beautify it than those arts which are called mathematical, unto the knowledge of which no man can attain, without perfect knowledge and instruction of the principles, grounds, and Elements of Geometry.

John Dee

All possible definitions of probability fall short of the actual practice.

William Feller

Nothing is more important than to see the sources of invention which are, in my opinion more interesting than the inventions themselves.

Gottfried Wilhelm von Leibniz

Miracles are not to be multiplied beyond necessity. Gottfried Wilhelm von Leibniz

Statistics: The only science that enables different experts using the same figures to draw different conclusions. Evan Esar

I have hardly ever known a mathematician who was capable of reasoning.

Plato

-				
	1	\mathbf{F}	(1861) Ivar Otto Bendixson	
			(1881) Otto Toeplitz	
			(1955) Bernadette Perrin-Riou	
	2	\mathbf{S}	(1856) Ferdinand Rudio	
			(1902) Mina Spiegel Rees	
	3	\mathbf{S}	(1914) Mark Kac	RM115
32	4	Μ	(1805) Sir William Rowan Hamilton	RM079
			(1838) John Venn	
	5	Т	(1802) Niels Henrik Abel	RM055
			(1941) Alexander Keewatin Dewdney	
	6	w		
			(1741) John Wilson	
	7	Т	(1868) Ladislaus Josephowitsch Bortkiewitz	
	8	F	(1902) Paul Adrien Maurice Dirac	RM103
	U	•	(1931) Sir Roger Penrose	1001100
	9	\mathbf{S}	(1537) Francesco Barozzi (Franciscus Barocius)	
	5	0	(1940) Linda Goldway Keen	
	10	\mathbf{S}	(1602) Gilles Personne de Roberval	
	10	D	(1926) Carol Ruth Karp	
33	11	М	(1730) Charles Bossut	
00	11	141	(136) Charles Bossut (1842) Enrico D'Ovidio	
	12	т	(1842) Jules Antoine Richard	
	14	1	(1882) Suies Antoine Kichard (1887) Erwin Rudolf Josef Alexander Schrödinger	RM103
	13	w	(1625) Erasmus Bartholin	1001100
	10	**	(1819) George Gabriel Stokes	
			(1861) Cesare Burali-Forti	
	14	т	(1530) Giovanni Battista Benedetti	
	11	1	(1842) Jean Gaston Darboux	
			(1865) Guido Castelnuovo	
			(1866) Charles Gustave Nicolas de La Vallée-Poussin	
	15	F	(1863) Aleksei Nikolaevich Krylov	
	10	•	(1892) Louis Pierre Victor Duc de Broglie	RM175
			(1901) Piotr Sergeevich Novikov	1001170
	16	\mathbf{S}	(1773) Louis-Benjamin Francoeur	
	10	2	(1821) Arthur Cayley	
	17	\mathbf{S}	(1601) Pierre de Fermat	RM091
34	18		(1685) Brook Taylor	1011001
01	19	Т	(1646) John Flamsteed	
	10	•	(1739) Georg Simon Klugel	
	20	w	(1710) Thomas Simpson	
	20	••	(1863) Corrado Segre	
			(1882) Wacłav Sierpiński	
	21	Т	(1789) Augustin Louis Cauchy	RM127
	22	F	(1647) Denis Papin	10111141
	23	S	(1683) Giovanni Poleni	
	20	5	(1829) Moritz Benedikt Cantor	
			(1823) Monte Benedikt Canton (1842) Osborne Reynolds	
	24	\mathbf{S}	(1561) Bartholomeo Pitiscus	
	44	5	(1942) Karen Keskulla Uhlenbeck	RM163
35	25	м	(1561) Philip Van Lansberge	10111100
00	-0	111	(1844) Thomas Muir	
	26	Т	(1728) Johann Heinrich Lambert	
1	-0		(1726) Johann Hennich Lämbert (1875) Giuseppe Vitali	
			(1965) Marcus Peter Francis du Sautoy	
	27	w	(1858) Giuseppe Peano	RM067
1	21 28		(1796) Irénée Jules Bienaymé	1001
1	28 29	F	(1904) Leonard Roth	
1				
1	30	\mathbf{S}	(1856) Carle David Tolmé Runge	DM100
1	01	C	(1906) Olga Taussky-Todd	RM139
1	31	\mathbf{S}	(1821) Hermann Ludwig Ferdinand von Helmholtz	
L			(1885) Herbert Westren Turnbull	





Putnam 1999, B2

Let P(x) be a polynomial of degree *n* such that $P(x)=Q(x)\cdot P''(x)$, where Q(x) is a quadratic polynomial and P''(x) is the second derivative of P(x). Show that if P(x) has at least two distinct roots then it must have n distinct roots. XX 200

The Amazing U

"You can do this in a number of ways. IBM chose to do all of them. Why do you find that funny?"

- D. Taylor Computer Science 350 CX 200

Weird, but true

A lottery is a tax on people who don't understand statistics.

Who would not rather have the fame of Archimedes than that of his conqueror Marcellus?

 \odot

Sir William Rowan Hamilton

Absolutely fundamental to the structure of quantum mechanics, complex numbers are so basic to the functioning of the world in which we live. They are also one of the great miracles of mathematics.

Sir Roger Penrose

Newton is, of course, the greatest of all teachers of Cambridge, but is also the biggest disaster ever happened not only to mathematicians at Cambridge in particular, but the whole British mathematical science.

Leonard Roth

Any form of mathematical thinking was created by Euler. It is only with great difficulty that you can follow the writings of any author preceding Euler, because you did not yet know how to make formulas talk for themselves. This art was taught first by Euler.

Ferdinand Rudio

Attaching significance to invariants is an effort to recognize what, because of its form or colour or meaning or otherwise, is important or significant and what is only trivial or ephemeral. A simple instance of failing in this is provided by the poll-man at Cambridge, who learned perfectly how to factorize $a^2 - b^2$ but was floored because the examiner unkindly asked for the factors of $p^2 - q^2$. H.W. Turnbull

35	1	М	(1659) Joseph Saurin	
99	1	IVI	(1835) William Stanley Jevons	
	2	Т	(1878) Mauriche René Frechet	
			(1923) René Thom	RM080
	3	W	(·) · · · · · · · · · · · · · · · · ·	RM104
			(1884) Solomon Lefschetz	
	4	т	(1908) Lev Semenovich Pontryagin (1809) Luigi Federico Menabrea	RM150
	+ 5	F	(1667) Giovanni Girolamo Saccheri	RM128
	0	-	(1725) Jean Etienne Montucla	1000120
	6	\mathbf{S}	(1859) Boris Jakovlevich Bukreev	
	_	~	(1863) Dimitri Aleksandrovich Grave	
	7	\mathbf{S}	(1707) George Louis Leclerc Comte de Buffon (1948) Cheryl Elisabeth Praeger	
			(1948) Cheryl Elisabeth Praeger (1955) Efim Zelmanov	
36	8	Μ	(1584) Gregorius Saint-Vincent	
			(1588) Marin Mersenne	RM092
	9	Т	(1860) Frank Morley	
	10		(1914) Marjorie Lee Browne	DM100
	10	W		RM123
	11	Т	(1623) Stefano degli Angeli (1798) Franz Ernst Neumann	
			(1877) Sir James Hopwood Jeans	
	12	\mathbf{F}	(1891) Antoine André Louis Reynaud	
			(1900) Haskell Brooks Curry	
	13	\mathbf{S}	(1894) Dorothy Maud Wrinch (1873) Constantin Carathéodory	
	10	N	(1885) Wilhelm Johann Eugen Blaschke	
	14	\mathbf{S}	(1858) Henry Burchard Fine	
			(1891) Ivan Matveevich Vinogradov	
37	15	М	(973) Abu Arrayhan Muhammad Ibn Ahmad Al'Biruni (1886) Paul Pierre Levy	RM164
	16	т	(1494) Francisco Maurolico	
			(1736) Johann Nikolaus Tetens	
	17	W		RM176
			Condorcet	DMOGO
	18	т	(1826) Georg Friedrich Bernhard Riemann (1752) Adrien Marie Legendre	RM068 RM140
	19	F	(1749) Jean Baptiste Delambre	1001140
	20	\mathbf{S}	(1842) Alexander Wilhelm von Brill	
			(1861) Frank Nelson Cole	
	21	\mathbf{S}	(1899) Juliusz Pawel Schauder	
38	22	М	(1917) Phyllis Nicolson (1765) Paolo Ruffini	RM116
			(1769) Louis Puissant	1000110
			(1803) Jaques Charles Francois Sturm	
	23	Т	(1768) William Wallace	
	24	w	(1900) David Van Dantzig (1501) Girolamo Cardano	RM064
	44	**	(1625) Johan de Witt	10004
			(1801) Michail Vasilevich Ostrogradski	RM056
			(1862) Winifred Edgerton Merrill	
	05	т	(1945) Ian Nicholas Stewart (1819) George Salmon	
	25	Т	(1819) George Salmon (1888) Stefan Mazurkiewicz	
	26	\mathbf{F}	(1688) Willem Jakob 's Gravesande	
			(1854) Percy Alexander Macmahon	
	o -	C	(1891) Hans Reichenbach	
	27	\mathbf{S}	(1855) Paul Émile Appell (1876) Earle Raymond Hedrick	
			(1919) James Hardy Wilkinson	
	28	\mathbf{S}	(1698) Pierre Louis Moreau de Maupertuis	RM152
			(1761) Ferdinand Francois Desirè Budan de Boislaurent	
			(1873) Julian Lowell Coolidge	
90	90	ЪЛ	(1501) Admission Van Deeman	
39	29	М		
39	29 30	M T	(1561) Adriaan Van Roomen (1812) Adolph Gopel (1775) Robert Adrain	
39			(1812) Adolph Gopel	

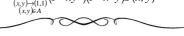




Putnam 1999, B3

Let $A=\{(x,y): 0 \le x, y \le 1\}$. For $(x,y) \in A$, let $S(x,y) = \sum_{\substack{1 \le m \le 2\\n}} x^m y^n$

where the sum ranges over all the pairs (m,n) of positive integers satisfying the indicated equalities. Evaluate $\lim_{\substack{(x,y) \to (1,1) \\ (x,y) \in A}} (1-xy^2)(1-x^2y)S(x,y)$



The Amazing U

"This process can check if this value is zero, and if it is, it does something child-like."

- Forbes Burkowski Computer Science 454

Weird, but true

A statistician is someone who is skilled at drawing a precise line from an unwarranted assumption to a foregone conclusion.

To throw in a fair game at Hazards only three-spots, when something great is at stake, or some business is the hazard, is a natural occurrence and deserves to be so deemed; and even when they come up the same way for a second time if the throw be repeated. If the third and fourth plays are the same, surely there is occasion for suspicion on the part of a prudent man.

Girolamo Cardano

The essential fact is that all the pictures which science now draws of nature, and which alone seem capable of according with observational facts, are mathematical pictures.

Sir James Hopwood Jeans

The greatest reward lies in making the discovery; recognition can add little or nothing to that.

Franz Ernst Neumann

...mathematics is distinguished from all other sciences except only ethics, in standing in no need of ethics. Every other science, even logic, especially in its early stages in danger of evaporating into airy nothingness, degenerating, as the Germans say, into an arachnoid film, spun from the stuff that dreams are made of. There is no such danger for pure mathematics; for that is precisely what mathematics ought to be.

Charles Sanders Peirce

...there is no study in the world which brings into more harmonious action all the faculties of the mind than [mathematics], ... or, like this, seems to raise them, by successive steps of initiation, to higher and higher states of conscious intellectual being....

James Joseph Sylvester

	1	W		RM177
			(1898) Bela Kerekjarto'	
	2	т	(1912) Kathleen Timpson Ollerenshaw (1825) John James Walker	
	4	1	(1908) Arthur Erdélyi	
	3	F	(1944) Pierre René Deligne	
	4	\mathbf{S}	(1759) Louis Francois Antoine Arbogast	
			(1797) Jerome Savary	
	5	\mathbf{S}	(1732) Nevil Maskelyne	D
			(1781) Bernhard Placidus Johann Nepomuk Bolzano (1861) Thomas Little Heath	RM117
40	6	м	(1561) Thomas Little Heath (1552) Matteo Ricci	RM141
10	U		(1831) Julius Wilhelm Richard Dedekind	RM081
			(1908) Sergei Lvovich Sobolev	
	7	Т	(1885) Niels Bohr	RM063
	8	W	(1908) Hans Arnold Heilbronn	
	9	Т	(1581) Claude Gaspard Bachet de Meziriac (1704) Johann Andrea von Segner	
			(1704) Johann Andrea von Segner (1873) Karl Schwarzschild	RM153
			(1949) Fan Rong K Chung Graham	RM1100
	10	\mathbf{F}	(1861) Heinrich Friedrich Karl Ludwig Burkhardt	
	11	\mathbf{S}	(1675) Samuel Clarke	
			(1777) Barnabè Brisson	
			(1881) Lewis Fry Richardson (1885) Alfred Haar	
			(1900) Cahit Arf	
	12	\mathbf{S}	(1860) Elmer Sperry	
41	13	М	(1890) Georg Feigl	
			(1893) Kurt Werner Friedrich Reidemeister	
	14	m	(1932) John Griggs Thomson	
	14	Т	(1687) Robert Simson (1801) Joseph Antoine Ferdinand Plateau	
			(1868) Alessandro Padoa	
	15	W	(1608) Evangelista Torricelli	RM165
			(1735) Jesse Ramsden	
			(1776) Peter Barlow	
	16	Т	(1931) Eléna Wexler-Kreindler (1879) Philip Edward Bertrand Jourdain	
	10	F	(1759) Jacob (II) Bernoulli	RM093
	11	1	(1888) Paul Isaac Bernays	100000
	18	\mathbf{S}	(1741) John Wilson	
			(1945) Margaret Dusa Waddington Mcduff	
	19	\mathbf{S}	(1903) Jean Frédéric Auguste Delsarte	DM170
42	20	м	(1910) Subrahmanyan Chandrasekhar (1632) Sir Christopher Wren	RM153 RM105
42	20	IVI	(1863) William Henry Young	U M109
			(1865) Aleksandr Petrovich Kotelnikov	
	21	Т	(1677) Nicolaus (I) Bernoulli	RM093
			(1823) Enrico Betti	RM150
			(1855) Giovan Battista Guccia (1802) William Leanand Ferman	RM129
			(1893) William Leonard Ferrar (1914) Martin Gardner	RM137
1	22	w	(1514) Martin Gardner (1587) Joachim Jungius	1011107
	-		(1895) Rolf Herman Nevanlinna	
			(1907) Sarvadaman Chowla	
	23	Т	(1865) Piers Bohl	
	24	F	(1804) Wilhelm Eduard Weber (1873) Edmund Taylor Whittaker	
	25	\mathbf{S}	(1873) Edmund Taylor Whittaker (1811) Évariste Galois	RM069
	26	\mathbf{s}	(1849) Ferdinand Georg Frobenius	1111000
1			(1857) Charles Max Mason	
<u> </u>			(1911) Shiing-Shen Chern	
43	27	М	(1678) Pierre Remond de Montmort	
	28	Т	(1856) Ernest William Hobson (1804) Pierre François Verhulst	
	20 29	W	(1925) Klaus Roth	
	30	Т	(1906) Andrej Nikolaevich Tichonov	
1	-		(1946) William Paul Thurston	
1	31	\mathbf{F}	(1711) Laura Maria Catarina Bassi	
			(1815) Karl Theodor Wilhelm Weierstrass	RM057 BM110
L			(1935) Ronald Lewis Graham	RM110





Putnam 1999, B4

Let *f* be a real function with a continuous third derivative such that f(x), f'(x), f''(x), f'''(x) are positive for all *x*. Suppose that $f'''(x) \le f(x)$ for all *x*. Show that f(x) < 2 f(x) for all *x*.

The Amazing U

"I think it is true for all n. I was just playing it safe with $n \ge 3$ because I couldn't remember the proof."

- Baker Pure Math 351a

Weird, but true

A statistician always has something to say with numbers while a politician has to say something with numbers.

Numbers are the free creation of the human mind. Julius Wilhelm Richard Dedekind

There is still a difference between something and nothing, but it is purely geometrical and there is nothing behind the geometry.

Martin Gardner

Gelfand amazed me by talking of mathematics as though it were poetry. He once said about a long paper bristling with formulas that it contained the vague beginnings of an idea which he could only hint at and which he had never managed to bring out more clearly. I had always thought of mathematics as being much more straightforward: a formula is a formula, and an algebra is an algebra, but Gelfand found hedgehogs lurking in the rows of his spectral sequences!

Margaret Dusa Waddington Mcduff

Another advantage of a mathematical statement is that it is so definite that it might be definitely wrong; and if it is found to be wrong, there is a plenteous choice of amendments ready in the mathematicians' stock of formulae. Some verbal statements have not this merit; they are so vague that they could hardly be wrong, and are correspondingly useless.

Lewis Fry Richardson

Numbers rule the universe.

Pitagoras

Mathematical demonstrations being built upon the impregnable Foundations of Geometry and Arithmetick are the only truths that can sink into the Mind of Man, void of all Uncertainty; and all other Discourses participate more or less of Truth according as their Subjects are more or less capable of Mathematical Demonstration.

Sir Christopher Wren

	-	a		
	1	S	(1535) Giambattista della Porta	DM004
	2	\mathbf{S}	(1815) George Boole (1896) Hanny John Stanhan Smith	RM094
4.4	0	м	(1826) Henry John Stephen Smith (1867) Martin Wilhelm Kutta	
44	3	М	(1867) Martin Wineim Kutta (1878) Arthur Byron Coble	
			(1876) Raymond Louis Wilder	
			(1906) Carl Benjamin Boyer	
	4	т	(1744) Johann (III) Bernoulli	RM093
	Ŧ		(1865) Pierre Simon Girard	100000
	5	w	(1848) James Whitbread Lee Glaisher	
	0	••	(1930) John Frank Adams	
	6	Т	(1781) Giovanni Antonio Amedeo Plana	RM154
			(1906) Emma Markovna Trotskaia Lehmer	
	7	\mathbf{F}	(1660) Thomas Fantet de Lagny	
			(1799) Karl Heinrich Graffe	
			(1898) Raphael Salem	
	8	\mathbf{S}	(1656) Edmond Halley	
			(1846) Eugenio Bertini	
			(1848) Fredrich Ludwig Gottlob Frege	
			(1854) Johannes Robert Rydberg	D1 (4 = 0
		~	(1869) Felix Hausdorff	RM178
	9	\mathbf{S}	(1847) Carlo Alberto Castigliano	
			(1885) Theodor Franz Eduard Kaluza	DMOOR
			(1885) Hermann Klaus Hugo Weyl (1906) Jaroslav Borisovich Lopatynsky	RM082
			(1906) Jaroslav Borisovich Lopatynsky (1913) Hedwig Eva Maria Kiesler (Hedy Lamarr)	RM144
			(1915) Hedwig Eva Maria Klesler (Hedy Lamarr) (1922) Imre Lakatos	10101144
45	10	м	(1829) Helwin Bruno Christoffel	
	11	Т	(1904) John Henry Constantine Whitehead	
	12	w		
			(1842) John William Strutt Lord Rayleigh	
			(1927) Yutaka Taniyama	
	13	Т	(1876) Ernest Julius Wilkzynsky	
			(1878) Max Wilhelm Dehn	
	14	\mathbf{F}	(1845) Ulisse Dini	
			(1919) Paulette Libermann	
	15	\mathbf{S}	(1688) Louis Bertrand Castel	
			(1793) Michel Chasles	
	16	e	(1794) Franz Adolph Taurinus (1835) Eugenio Beltrami	RM150
46	<u>16</u> 17	S M		RM150
40	17	IVI	(1717) Jean Le Rond D'Alembert	RM166
			(1790) August Ferdinand Möbius	RM1100
	18	Т	(1872) Giovanni Enrico Eugenio Vacca	1001110
	10	-	(1927) Jon Leslie Britton	
	19	w	(1894) Heinz Hopf	
			(1900) Michail Alekseevich Lavrentev	
			(1901) Nina Karlovna Bari	
	20	Т	(1889) Edwin Powell Hubble	
			(1924) Benoît Mandelbrot	
			(1963) William Timothy Gowers	
	21		(1867) Dimitri Sintsov	
	22	\mathbf{S}	(1803) Giusto Bellavitis	
		~	(1840) Émile Michel Hyacinthe Lemoine	D340=0
	23	\mathbf{S}	(1616) John Wallis	RM070
			(1820) Issac Todhunter (1917) Elizabeth Leonard Scott	DM100
47	24	м	(1917) Elizabeth Leonard Scott (1549) Duncan Maclaren Young Sommerville	RM106
41	24	IVL	(1549) Duncan Maclaren Young Sommerville (1909) Gerhard Gentzen	
	25	т	(1841) Fredrich Wilhelm Karl Ernst Schröder	
	20	1	(1873) Claude Louis Mathieu	
			(1943) Evelyn Merle Roden Nelson	
	26	W	(1894) Norbert Wiener	RM172
			(1946) Enrico Bombieri	
	27	Т	(1867) Arthur Lee Dixon	
		Б	(1898) John Wishart	
1	28	\mathbf{F}		
	28 29	r S	(1803) Christian Andreas Doppler	
			(1849) Horace Lamb	
	29	\mathbf{S}	(1849) Horace Lamb (1879) Nikolay Mitrofanovich Krylov	
		\mathbf{S}	(1849) Horace Lamb	RM142





Putnam 1999, B5

For an integer $n \ge 3$, let $\theta = 2\pi/n$. Evaluate the determinant of the matrix $I_n + A_n$, where I_n is the identity matrix and A_n is the square matrix with entries: $a_{jk} = \cos(j\theta + k\theta)$.



The Amazing U

"Now this is a totally brain damaged algorithm. Gag me with a smurfette."

- P. Buhr Computer Science 354.

Weird, but true

Statisticians are like the drunk leaning against the lamp pole: they are there for support, not illumination.

Whoever hates mathematics as a child will do for all his life. Nobody wakes up one day enlightened by love for such a discipline.

Enrico Bombieri

The mathematician may be compared to a designer of garments, who is utterly oblivious of the creatures whom his garments may fit. To be sure, his art originated in the necessity for clothing such creatures, but this was long ago; to this day a shape will occasionally appear which will fit into the garment as if the garment had been made for it. Then there is no end of surprise and delight.

George Dantzig

It is the peculiar beauty of this method, gentlemen, and one which endears it to the really scientific mind, that under no circumstance can it be of the smallest possible utility.

Henry John Stephen Smith

We are not very pleased when we are forced to accept a mathematical truth by virtue of a complicated chain of formal conclusions and computations, which we traverse blindly, link by link, feeling our way by touch. We want first an overview of the aim and of the road; we want to understand the idea of the proof, the deeper context.

Hermann Klaus Hugo Weyl

Progress imposes not only new possibilities for the future but new restrictions.

Norbert Wiener

There is nothing mysterious, as some have tried to maintain, about the applicability of mathematics. What we get by abstraction from something can be returned. Raymond Louis Wilder

48	1	М	(1792) Nikolay Yvanovich Lobachevsky	RM083
		-	(1847) Christine Ladd-Franklin	
	2	Т	(1831) Paul David Gustav du Bois-Reymond	
	3	w	(1901) George Frederick James Temple (1903) Sidney Goldstein	
	0		(1924) John Backus	
	4	Т	(1795) Thomas Carlyle	
	5	\mathbf{F}	(1868) Arnold Johannes Wilhelm Sommerfeld	
			(1901) Werner Karl Heisenberg	RM155
	0	a	(1907) Giuseppe Occhialini	RM122
	6 7	\mathbf{s}	(1682) Giulio Carlo Fagnano dei Toschi (1647) Giovanni Ceva	
	'	0	(1823) Leopold Kronecker	
			(1830) Antonio Luigi Gaudenzio Giuseppe Cremona	RM150
			(1924) Mary Ellen Rudin	
49	8	М	(1508) Regnier Gemma Frisius	
			(1865) Jaques Salomon Hadamard	
	9	т	(1919) Julia Bowman Robinson (1883) Nikolai Nikolaievich Luzin	
	5	1	(1906) Grace Brewster Murray Hopper	
			(1917) Sergei Vasilovich Fomin	
	10	W	(1804) Karl Gustav Jacob Jacobi	
		-	(1815) Augusta Ada King Countess Of Lovelace	RM059
	11	Т	(1882) Max Born	RM155
	$\frac{12}{13}$	F S	(1832) Peter Ludwig Mejdell Sylow (1724) Franz Ulrich Theodosius Aepinus	
	10	0	(1724) Franz Onten Theodosius Aepinus (1887) George Polya	RM131
	14	\mathbf{S}	(1546) Tycho Brahe	1011101
50	15	М	(1802) János Bolyai	RM083
			(1923) Freeman John Dyson	
	16	Т	(1804) Wiktor Yakovievich Bunyakowsky	
	17	W	(1706) Gabrielle Emile Le Tonnelier de Breteuil du Chatelet	
			(1835) Felice Casorati	
			(1842) Marius Sophus Lie	
			(1900) Dame Mary Lucy Cartwright	
	18	Т	(1856) Joseph John Thomson	RM161
			(1917) Roger Lyndon (1942) Lenore Blum	
	19	F	(1783) Charles Julien Brianchon	
	10	-	(1854) Marcel Louis Brillouin	
			(1887) Charles Galton Darwin	RM138
	20	\mathbf{S}	(1494) Oronce Fine	
			(1648) Tommaso Ceva (1875) Francesco Paolo Cantelli	
	21	\mathbf{S}	(1878) Jan Łukasiewicz	
	41	D	(1921) Edith Hirsch Luchins	
			(1932) John Robert Ringrose	
51	22	М	(1824) Francesco Brioschi	RM150
1			(1859) Otto Ludwig Hölder	
1			(1877) Tommaso Boggio (1887) Srinivasa Aiyangar Ramanujan	
1	23	Т	(1872) Georgii Yurii Pfeiffer	
1	24	w	(1822) Charles Hermite	RM095
1			(1868) Emmanuel Lasker	RM167
1	25	Т	(1642) Isaac Newton	RM071
1	26	F	(1900) Antoni Zygmund (1780) Mary Fairfax Greig Somerville	
	20	Ľ	(1791) Charles Babbage	RM059
			(1937) John Horton Conway	RM119
1	27	\mathbf{S}	(1571) Johannes Kepler	
1		~	(1654) Jacob (Jacques) Bernoulli	RM093
1	28	\mathbf{S}	(1808) Athanase Louis Victoire Duprè	DM170
1			(1882) Arthur Stanley Eddington (1903) John von Neumann	RM179 RM107
52	29	М	(1856) Thomas Jan Stieltjes	1011101
	30	Т	(1897) Stanislaw Saks	
	31	W	(1872) Volodymyr Levitsky	
1			(1896) Carl Ludwig Siegel (1945) Leonard Adleman	DM140
1			(1945) Leonard Adleman (1952) Vaughan Frederick Randall Jones	RM143
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Putnam 1999, B6

Let S be a finite set of integers, each greater than 1. Suppose that for each integer n there is some $s \in S$ such that MCD(s,n)=1 or MCD(s,n)=s. Show that there exist $(s,t)\in S$ such that MCD(s,t) is prime.

The Amazing U

"How do you find an isomorphism? You just f it. See? Graph theory is a lot of fun."

- I. Goulden Combinatorics and Optimization 230

Weird, but true

Life, Math & Everything Life is complex. It has real and imaginary components.

To a Mathematician, real life is a special case.

If God has made the world a perfect mechanism, He has at least conceded so much to our imperfect intellect that in order to predict little parts of it, we need not solve innumerable differential equations, but can use dice with fair success.

Max Born

We have found a strange footprint on the shores of the unknown. We have devised profound theories, one after another, to account for its origins. At last, we have succeeded in reconstructing the creature that made the footprint. And lo! It is our own.

Arthur Stanley Eddington

Practical application is found by not looking for it, and one can say that the whole progress of civilization rests on that principle.

Jaques Salomon Hadamard

Abel has left mathematicians enough to keep them busy for 500 years.

Charles Hermite

Temporis filia veritas; cui me obstetricari non pudet. (Truth is the daughter of time, and I feel no shame in being her midwife.)

Johannes Kepler

What good your beautiful proof on [the transcendence of] π ? Why investigate such problems, given that irrational numbers do not even exist?

Leopold Kronecker

We can affirm that the Analytical Engine of Mr. Babbage weaves algebraic patterns, just as the Jacquard loom weaves flowers and leaves.

Augusta Ada King Countess Of Lovelace